

CLASS-9 PHYSICS

Ch-4 , PRESSURE IN FLUIDS

NUMERICAL PROBLEMS (page no -74)

Q1- Calculate the pressure on a circular area of 100 cm^2 in a water of 100m deep. (Density of water $=10^3\text{kg/m}^3$ and $g= 10 \text{ m/s}^2$)

Solution- Area= 100cm^2

Depth(h)= 100m

Density of water= 10^3kg/m^3

G= 10 m/s^2

Pressure = depth \times density \times acc.due to gravity

$$\begin{aligned}\text{Pressure} &= 100 \times 10^3 \times 10 \\ &= 10^6 \text{N/m}^2\end{aligned}$$

Q2- Calculate the force acting on the circular area in the above program.

Solution- force acting= Area \times depth \times density \times acc.due to gravity

$$\begin{aligned}\text{Force} &= 100/10000 \times 100 \times 10^3 \times 10 \\ &= 10^4 \text{N}\end{aligned}$$

Q3- A hammer exerts a force of 1.5 N on a nail of tip area 2mm^2 . Calculate the pressure on the nail.

Solution- force= 1.5N

Area= $2\text{mm}^2= 0.000002\text{m}^2$

Pressure= force/area

$$\begin{aligned}&= 1.5\text{N}/0.000002\text{m}^2 \\ &= 7.5 \times 10^5 \text{ pa}\end{aligned}$$

Q4- A wooden block of mass 7.5 kg of size $12\text{cm} \times 8\text{cm} \times 10\text{cm}$ is kept on a table top on its $12\text{cm} \times 8 \text{ cm}$. Calculate (i) thrust (ii) pressure exerted on the top of table

Solution- mass = 7.5 kg

Area of table= $(12 \times 8)\text{cm}^2= 96 \text{ cm}^2= 0.0096 \text{ m}^2$

(i) thrust = $m \times g$

$$7.5 \times 10 = 75\text{N}$$

(ii) pressure= force / area

$$= 75 \times 0.0096$$

$$= 7812.5 \text{ pa}$$

Q5- The area of base of a cylinder vessel is 0.03 m^2 . Water density 10^3 kg/m^3 is poured into it upto a depth of 6 cm . Calculate (i) pressure .

(ii) thrust of water on the base ($g = 10 \text{ m/s}^2$)

Solution- area = 0.03 m^2

Density of water(d)= 10^3 kg/m^3

$h = 6 \text{ cm} = 0.06 \text{ m}$

$g = 10 \text{ m/s}^2$

(i) pressure= depth \times density \times g

$$0.06 \times 10^3 \times 10$$

$$= 600 \text{ pa}$$

(ii) thrust = $A \times h \times d \times g$

$$0.03 \times 0.06 \times 10^3 \times 10$$

$$= 18 \text{ N}$$

Q6- Calculate the height of of water column which will exerts on its base the same pressure as the 0.70 m of mercury column. Density of Hg is $13.6 \times 10^3 \text{ kg/m}^3$.

Solution- for water column

Let pressure= P_1

Height = h_1 .

Density = $D_1 = 10^3 \text{ kg/m}^3$

And acc. due to gravity= g

Then , $P_1 = h_1 \times 10^3 \text{ kg/m}^3 \times g$

Now ,for Mercury column

Let pressure= P_2

Height of mercury column= $h_2 = 0.70 \text{ m}$

Density= $D_2 = 13.6 \times 10^3 \text{ kg/m}^3$

Acc. Due to gravity = g

Now $P_1 = P_2$

$$h_1 \times 10^3 \text{kg/m}^3 \times g = 0.70 \text{m} \times 13.6 \times 10^3 \text{kg/m}^3 \times g$$

$$h_1 = 0.70 \text{m} \times 13.6$$

$$h_1 = 9.52 \text{m}$$

Q7- The. Pressure difference between two floors of a building is 30000 pascal. Find the vertical distance between the floors (density = 10^3kg/m^3 , $g = 10 \text{m/s}^2$)

Solution- pressure difference = 30000 Pascal

$$\text{Density of water} = 10^3 \text{kg/m}^3.$$

$$g = 10 \text{m/s}^2$$

We know, pressure = $h \times \text{density} \times g$

$$30000 = h \times 10^3 \times 10$$

$$h = 3 \text{m}$$

Q8- In a hydraulic machine a force of 20 N is applied on the piston of area 10cm^2 . What force is obtained on its piston of area 100cm^2 .

Solution- $F_1 = 20 \text{N}$

$$A_1 = 10 \text{cm}^2$$

$$F_2 = ?$$

$$A_2 = 100 \text{cm}^2$$

We know $P_1 = P_2$

$$\text{So, } F_1/A_1 = F_2/A_2$$

$$f_2 = f_1 \times A_2/A_1$$

$$F_2 = 20 \times 100/10$$

$$f_2 = 200 \text{N}$$

Q9- Calculate the ratio of area cross section of master cylinder and wheel cylinder of hydraulic brake so that a force of 10N can be obtained at each of its brake shoe by exerting a force of 0.2N on the pedal.

Solution- for master cylinder

$$A_1 = ?$$

$$F_1 = 0.2 \text{N}$$

For wheel cylinder

$$A_2 = ?$$

$$F_2 = 10\text{N}$$

When $P_1 = P_2$

$$A_1/A_2 = F_1/f_2$$

$$A_1/A_2 = 0.2/100$$

$$A_1:A_2 = 1:50$$

Q10- The area of pistons in a hydraulic machine are 5cm^2 and 125cm^2 . What force on smaller piston will support a load of 1000N on the large piston.

Solution- $A_1 = 5\text{cm}^2$

$$A_2 = 125\text{cm}^2$$

$$F_1 = ?$$

$$f_2 = 1000\text{N}$$

$$F_1 = f_2 \times A_1/A_2$$

$$f_2 = 1000 \times 5/125$$

$$f_2 = 40\text{N}$$

Q11- A force of 500N is applied to the smaller piston of a hydraulic machine. Find the force exerted on the large piston if the diameter of the piston are 5cm and 25cm .

Solution- $F_1 = 500\text{N}$

$$F_2 = ?$$

$$D_1 = 5\text{cm}, \text{ So radius } r = 5/2$$

$$\text{Therefore } A_1 = \pi \times (5/2)^2$$

$$A_1 = 25\pi/4$$

$$D_2 = 25\text{cm}, \text{ so radius} = 25/2$$

$$\text{Therefore. } A_2 = \pi \times (25/2)^2$$

$$A_2 = 625\pi/4$$

Now $f_2 = f_1 \times A_2/A_1$

$$f_2 = (500 \times 625\pi/4) \div 25\pi/4$$

$$f_2 = 12500\text{N}$$

Q12- What force is applied on a piston of area of cross section 2.0cm^2 to obtain a force of 240N on the piston of area 12.0cm^2 in a hydraulic machine.

Solution- $F_1 = ?$

$$A1 = 2\text{cm}^2$$

$$f2 = 240\text{N}$$

$$A2 = 12\text{cm}^2$$

$$F1 = F2 \times A1 / A2$$

$$F1 = 240 \times 2 / 12$$

$$F1 = 40\text{N}$$

PAGE NO-81 NUMERICALS

Q1- Calculate the hydrostatic pressure at the depth of 100m in a sea water and also total pressure at this depth .(Density of sea water $1.03 \times 10^3 \text{kg/m}^3$, atmospheric pressure= 10^5N/m^2 , $g = 10\text{m/s}^2$)

Solution- depth (h)= 100m

Density of sea water (d)= $1.03 \times 10^3 \text{kg/m}^3$

$$g = 10\text{m/s}^2$$

Now hydrostatic pressure= $h \times d \times g$

$$= 100 \times 1.03 \times 10^3 \times 10$$

$$= 10.3 \times 10^5 \text{pa}$$

Atmospheric pressure= 10^5N/m^2

Total pressure= hydrostatic pressure+ atmospheric pressure

Total pressure=($10.3 \times 10^5 + 10^5$)pa

$$= 11.3 \times 10^5 \text{pa}$$

Q2- same as numerical -6 of page no 74

Q3- The base of a cylindrical vessel is 300cm^2 .water is poured upto a depth of 7cm . Calculate the pressure on the base($g = 10\text{m/s}^2$, density of water= 10^3m/s^2)

Solution- Base area = 300cm^2

Depth of water (h) = $7\text{cm} = 0.07 \text{m}$

$$g = 10\text{m/s}^2$$

Density of water (d) = 10^3kg/m^3

Pressure at the base= $h \times d \times g$

Pressure= $0.07 \times 10^3 \times 10$

=700pa

Q4- Atmospheric pressure= 720mm of Hg

Density of mercury (d)= 13.6×10^3

$g = 10 \text{m/s}^2$

$h = 720 \text{mm} = 0.720 \text{m}$

Pressure= $h \times d \times g$

Pressure= $0.720 \times 13.6 \times 10^3 \times 10$

Pressure= 97920pa

Q5- Convert 2mm of mercury into N/m^2

(density of mercury= $13.6 \times 10^3 \text{kg/m}^3$, $g = 9.8 \text{m/s}^2$)

Solution- $h = 2 \text{mm} = 0.002 \text{m}$

Density of mercury (d)= $13.6 \times 10^3 \text{kg/m}^3$

$g = 9.8 \text{m/s}^2$

Pressure= $h \times d \times g$

Pressure= $0.002 \times 13.6 \times 10^3 \times 9.8$

Pressure= 266.56Nm^2